

**CBA-249-T****BCA First Semester  
(End Semester)****Examination Dec., 2018****COMPUTER SCIENCE AND APPLICATIONS****Paper - CSA-CC-115****(Maths for Computers Science)**

Time : Three Hours ]

[ Maximum Marks 60

Note :- Attempt all questions.

[ P. T. O.

**Section-A****(Objective Type Questions) 10x1=10**

1. Choose the correct option.
  - (i) The diagonal elements of skew-symmetric matrix are
    - (a) nonzero
    - (b) zero
    - (c) irrational
    - (d) none of these
  - (ii) If every minor of order  $n+1$  vanishes, then rank is
    - (a) less than  $n$
    - (b)  $n+1$
    - (c)  $\leq n$
    - (d) none of these

(iii)  $(\exists P \wedge (\exists Q \wedge R)) \vee (Q \wedge R) \vee (P \wedge R)$

is equivalent to

- (a)  $(\exists(P \vee Q) \vee (P \vee Q)) \wedge R$
- (b) R
- (c) both (a) and (b)
- (d) none of these

(iv) A statement A is said to tautologically imply a statement B if and only if

- (a)  $A \rightarrow B$  is a tautology
- (b)  $A \rightarrow B$  is not a tautology
- (c)  $B \rightarrow A$  is a tautology
- (d) None of these

(v) Let  $R = \{(a, b) : a + 3b = 12, a, b \in N\}$ , then domain of R is

- (a) {9, 3, 6}
- (b) {1, 2, 3}
- (c) {3, 1, 6}
- (d) {1, 2, 3, ...}

(vi) If  $\circ(x) = m, \circ(y) = n$ , then total number of functions from x to y are

- (a)  $m^n$
- (b)  $n^m$
- (c)  $m^m$
- (d)  $2^{m+n}$

(vii) A vertex in a graph is said to be pendent vertex if its degree is

- (a) zero
- (b) one
- (c) two
- (d) three

(viii) A null graph which consists of at least two vertices is a

- (a) connected graph
- (b) disconnected graph
- (c) strongly connected graph
- (d) none of these

(ix) If  $G = (V, E)$  is any connected graph, then  $T = (V, E)$  is a spanning tree of  $G$  if

- (a)  $T$  has the same vertex  $v$  of vertices as does  $G$
- (b)  $T$  is a tree
- (c)  $T$  is a subgraph
- (d) All of these

(x) The minimum height of a binary tree with 9 vertices is

- (a) 4
- (b) 6
- (c) 3
- (d) 2

#### Section 'B'

(Short Answer Type Questions)  $4 \times 5 = 20$

Note : Attempt any four questions

- 2 Show that the eigen values of symmetric matrix are real
- 3 Prove that  $\text{Rank}(A) = \text{Rank}(AT)$

- 4 Prove that  $(P \rightarrow (Q \rightarrow R)) \Leftrightarrow (P \rightarrow Q) \rightarrow (P \rightarrow R)$ .
- 5 If  $R^{-1}$  and  $S^{-1}$  are inverse of the relations  $R$  and  $S$  respectively, then prove that  $(SOR)^{-1} = R^{-1} \circ S^{-1}$
- 6 Prove that the vertices of odd degree in a graph is always even. <http://www.dhsgsu.com>
- 7 Express the algebraic expression  $(x - y) + ((y + z) + w)$  in a binary tree

#### Section 'C'

(Long Answer Type Questions)  $3 \times 10 = 30$

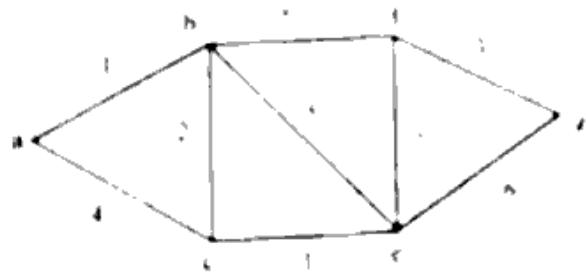
- 8 Solve the following equations with the help of
  - elementary operations of matrix method:

$$\begin{aligned}x + y + z &= 6 \\x - y + z &= 2 \\2x + y - z &= 1\end{aligned}$$

- 9 Construct the truth table for the formula
  - (i)  $\neg(P \wedge Q) \Leftrightarrow (\neg P \vee \neg Q)$
  - (ii)  $(P \rightarrow Q) \wedge (Q \rightarrow P)$

10 Show that the relation 'is divisor of' in the set of positive integers is reflexive and transitive, but not symmetric.

11 find the shortest path from a to z in the graph shown  
 • in figure where numbers associated with the edges are the weights



12 Prove that a tree with  $n$  vertices has  $(n-1)$  edges

